

Key

Operations with Complex Numbers

Simplify each expression. Identify matching answers between Column 1 and Column 2. Put the letter of the matching problem in the blank.

1. $(3 - 4i) + (2 + 5i)$ $5 + i$ (I)

2. $(8 + 7i) - (5 + 9i)$ $3 - 2i$ (K)
 $8 + 7i - 5 - 9i$

3. $2i(6 - 7i)$ $14 + 12i$ (C)
 $12i - 14i^2$

4. $-8i(2 + 7i) + 30i$ $56 + 14i$ (F)
 $-16i - 56i^2 + 30i$

5. $2i(7 + 3i) + 5(-5i)$ $-6 - 11i$ (A)
 $14i + 6i^2 - 25i$

6. $5i^{27}$ $-5i$ $5(i^2)^{13}i$ (J)

7. $(1 - 4i)(3 - 3i)$ $-9 - 15i$ (D)
 $3 - 3i - 12i + 12i^2$

8. $(1 - 5i)^2 - (8 - 4i)$ $-32 - 6i$ (G)
 $(1 - 5i)(1 - 5i) - 8 + 4i$
 $1 - 10i + 25i^2 - 8 + 4i$

9. $\frac{10 - 2i}{i}$ $-2 - 10i$ (B)
 $\frac{10i - 2i^2}{i^2} = \frac{10i + 2}{-1} = -10i - 2$

10. Solve: $x^2 - 6x + 25 = 0$ $3 \pm 4i$ (L)
 $\frac{-(-6) \pm \sqrt{36 - 4(1)(25)}}{2(1)} \rightarrow \frac{6 \pm \sqrt{-64}}{2} \rightarrow \frac{6 \pm 8i}{2} = 3 \pm 4i$

11. $\frac{4i}{-1+i}$ $2 - 2i$ (E)
 $\frac{4i}{-1+i} \cdot \frac{-1-i}{-1-i} = \frac{-4i - 4i^2}{1 - i^2} = \frac{4 - 4i}{2} = 2 - 2i$

12. $i^2 + i^5 + 1$ i (H)
 $-1 + (i^2)^2 i + 1$
 $-1 + (-1)^2 i + 1$
 $-1 + i + 1$

A. $(9 - 7i) - (15 + 4i)$
 $-6 - 11i$

B. $(-7 - 3i) + (5 - 7i)$
 $-2 - 10i$

C. $3i(4 - 5i) - 1$
 $12i - 15i^2 - 1 \rightarrow 12i + 15 - 1 = 14 + 12i$

D. $-2(3 - 4i) - (3 + 23i)$
 $-6 + 8i - 3 - 23i = -9 - 15i$

E. $3i(7 - 2i) + 2(-2 - 11i) - i$
 $21i - 6i^2 - 4 - 22i - i = 2 - 2i$

F. $8(9 + 3i) - 2(8 + 5i)$
 $72 + 24i - 16 - 10i = 56 + 14i$

G. $(2 - 4i)(-2 - 7i)$
 $-4 - 14i + 8i + 28i^2 = -32 - 6i$

H. i^{65}
 $(i^2)^{32}i = i$

I. $\frac{-1+5i}{i} \cdot \frac{i}{i} = \frac{-i+5i^2}{i^2} = \frac{-5-i}{-1} = 5+i$

J. $\frac{-10+5i}{-1-2i} \cdot \frac{-1+2i}{-1+2i} = \frac{10-20i-5i+10i^2}{1-4i^2} = \frac{-25i}{5} = -5i$

K. $\frac{-1-8i}{1-2i} \cdot \frac{1+2i}{1+2i} = \frac{-1-2i-8i-16i^2}{1-4i^2} = \frac{15-10i}{5} = 3-2i$

L. Solve: $(x - 3)^2 = -16$
 $x = 3 \pm 4i$