

# ① Solve by Factoring

a.

$$4x^2 - 81 = 0$$

$$(2x+9)(2x-9) = 0$$

4.5 and  
-4.5

b.

$$3x^2 + 22x = -9$$

$$3x^2 + 22x + 9 = 0$$

$$(x+9)(3x+1) = 0$$

$$x = -9 \quad x = -\frac{1}{3}$$

② Change each *function* into  
intercept form by  
factoring

a

$$y = 3x^2 - 4x + 1$$
$$y = (3x - 1)(x - 1)$$

$1\frac{1}{3}$

b

$$y = x^2 - 9x + 20$$

$$y = (x - 4)(x - 5)$$

③ Solve by taking the Square Root of Both Sides

a

$$\begin{aligned} (x+3)^2 + 1 &= 82 \\ \sqrt{(x+3)^2} &= \sqrt{81} \\ x+3 &= \pm 9 \end{aligned}$$

$$\begin{aligned} x &= -3 \pm 9 \\ x &= 6, -12 \end{aligned}$$

b

$$2(x-2)^2 = 50$$

$$(x-2)^2 = 25$$

$$x-2 = \pm 5$$

$$2 \pm 5$$

$$7, -3$$

④ Complete the Square  
to solve when  $a=1$

a

$$x^2 = -12x - 32$$

$$x^2 + 12x + \boxed{36} = -32 + \boxed{36}$$

$$\sqrt{(x+6)^2} = \sqrt{4}$$

$$x+6 = \pm 2$$

$$x = -6 \pm 2$$

$$\begin{aligned}x &= -8 \\&\text{or} \\x &= -4\end{aligned}$$

⑤ Complete the Square to Solve

when  $a \neq 1$

You cannot use  $(\frac{b}{2})^2$  when  $a \neq 1$ !

$$4x^2 + 20x + \boxed{25}$$

$$(2x+5)^2$$

$$(2x+5)(2x+5)$$

$$9x^2 - 12x + \boxed{4}$$

$$(3x-2)^2$$

$$3x^2 - 12x + 6 = 0$$
$$\underline{3x^2 - 12x} \quad = -6$$

$$x^2 - 4x + \boxed{4} = -2 + \boxed{4}$$
$$\sqrt{(x-2)^2} = \sqrt{2}$$
$$x-2 = \pm\sqrt{2}$$

$$x = 2 \pm \sqrt{2}$$

$$4x^2 - 8x - 32 = 0$$

$$x^2 - 2x - 8 = 0$$

$$x^2 - 2x + \boxed{1} = 8 + \boxed{1}$$

$$(x-1)^2 = 9$$

$$x-1 = \pm 3$$

$$x = 1 \pm 3$$

4 or -2

⑥ Complete the Square to put  
into vertex form.  
Then find the vertex.

a)  $y = x^2 + 12x + 32$

$$y = \boxed{x^2 + 12x + \boxed{36}} + 32 - \boxed{-36}$$

$$y = (x+6)^2 - 4$$

⑥ Complete the Square to put  
into vertex form.  
Then find the vertex.

⑥  $y = x^2 + 8x + 12$

$$y = x^2 + 8x + \boxed{16} + 12 + \boxed{-16}$$

$$y = (x+4)^2 - 4$$

$$\text{Vertex: } (-4, -4)$$

⑥ Complete the Square to put  
into vertex form.  
Then find the vertex.

c)  $y = 2x^2 + 12x - 4$

$$y = 2(x^2 + 6x + \boxed{9}) - 4 + \boxed{-18}$$

$$y = 2(x + 3)^2 - 22$$

⑤ Complete the Square to put  
into vertex form.  
Then find the vertex.

a)  $y = 3x^2 + 18x - 1$

$$y = 3 \left[ x^2 + 6x + \boxed{9} \right] - 1 + \boxed{-27}$$

$$y = 3(x+3)^2 - 28$$

⑤ Complete the Square to put  
into vertex form.  
Then find the vertex.

e)  $y = -2x^2 + 8x - 8$