

Graphing Quadratics Review

Use vertex form to write a quadratic equation from given points

Use each table to write a quadratic function in vertex form, $y = a(x - h)^2 + k$. Then rewrite the function in standard form, $y = ax^2 + bx + c$.

The vertex of the parabola is (2, 5).

x	y
-1	59
1	11
2	5
3	11
5	59

$$y = a(x-2)^2 + 5$$

$$11 = a(1-2)^2 + 5$$

$$11 = a + 5$$

$$6 = a$$

$$y = 6(x-2)^2 + 5$$

$$y = 6(x-2)(x-2) + 5$$

$$6(x^2 - 4x + 4) + 5$$

$$6x^2 - 24x + 24 + 5$$

$$y = 6x^2 - 24x + 29$$

The vertex of the parabola is (-2, -7).

x	y
0	-27
-1	-12
-2	-7
-3	-12
-4	-27

$$y = a(x+2)^2 - 7$$

$$-27 = 4a - 7$$

$$-20 = 4a$$

$$-5 = a$$

$$y = -5(x+2)^2 - 7$$

$$y = -5(x+2)(x+2) - 7$$

$$y = -5(x^2 + 4x + 4) - 7$$

$$y = -5x^2 - 20x - 20 - 7$$

$$y = -5x^2 - 20x - 27$$

The vertex of the function is (6, -8).

x	y
10	24
8	0
6	-8
4	0
2	24

$$y = a(x-6)^2 - 8$$

$$0 = a(2)^2 - 8$$

$$0 = 4a - 8$$

$$8 = 4a$$

$$2 = a$$

$$y = 2(x-6)^2 - 8$$

$$y = 2(x-6)(x-6) - 8$$

$$2(x^2 - 12x + 36) - 8$$

$$2x^2 - 24x + 72 - 8$$

$$y = 2x^2 - 24x + 64$$

The vertex of the function is (4, 7).

x	y
0	-1
2	5
4	7
6	5
8	-1

$$y = a(x-4)^2 + 7$$

$$-1 = a(-4)^2 + 7$$

$$-1 = 16a + 7$$

$$-8 = 16a$$

$$-\frac{1}{2} = a$$

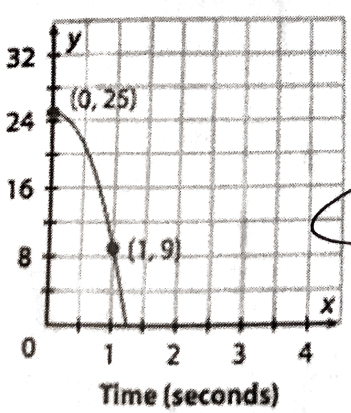
$$y = -\frac{1}{2}(x-4)^2 + 7$$

$$y = -\frac{1}{2}(x^2 - 8x + 16) + 7$$

$$-\frac{1}{2}x^2 + 4x - 8 + 7$$

$$y = -\frac{1}{2}x^2 + 4x - 1$$

A house painter standing on a ladder drops a paintbrush, which falls to the ground. The paintbrush's height above the ground (in feet) is given by a function of the form $f(t) = a(t - h)^2 + k$ where t is time (in seconds) after the paintbrush is dropped.



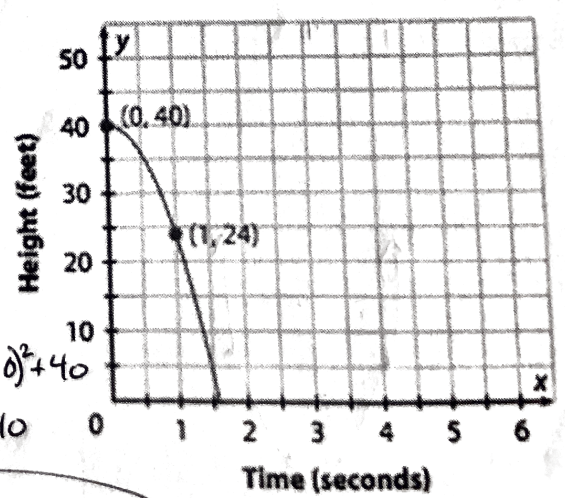
$$y = a(x-0)^2 + 25$$

$$9 = a(1)^2 + 25$$

$$a = -16$$

$$y = -16x^2 + 25$$

A rock is knocked off a cliff into the water far below. The falling rock's height above the water (in feet) is given by a function of the form $f(t) = a(t - h)^2 + k$ where t is the time (in seconds) after the rock begins to fall.



$$y = a(t-0)^2 + 40$$

$$24 = a + 40$$

$$-16 = a$$

$$y = -16t^2 + 40$$

Graphing Quadratics Review

1) $y = -2(x - 1)^2 + 5$

Axis of Symmetry is $x = 1$

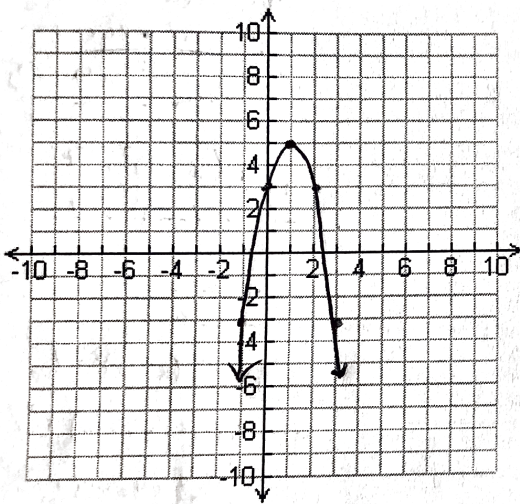
Vertex: $(1, 5)$

Opens up or down?

Find pts 1 unit L/R of vertex:

$(0, 3)$ and $(2, 3)$

y-intercept: $(0, 3)$



2) $y = 2x^2 - 8x + 6$ $a = 2$ $b = -8$ $c = 6$

Opens up or down?

Is vertex a ~~max~~ or min? because it opens up

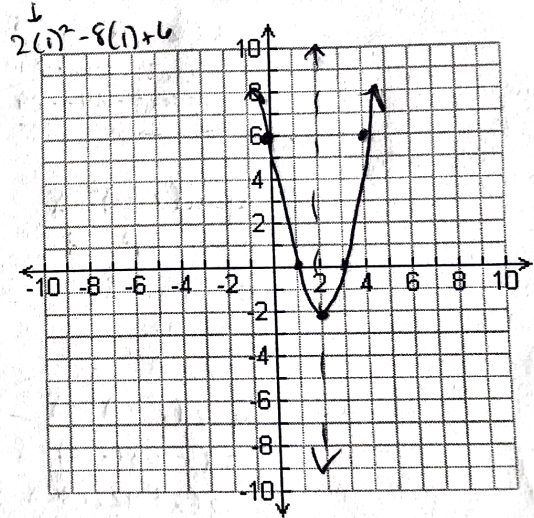
Y-intercept: $(0, 6)$

Axis of Symmetry is $x = 2$ $-\frac{(-8)}{2(2)} = \frac{8}{4} = 2$

Vertex: $(2, -2)$ $2(2)^2 - 8(2) + 6 = 8 - 16 + 6 = -2$

Find pts 1 unit L/R of vertex at

$(1, 0)$ and $(3, 0)$



3) $y = \frac{1}{2}(x - 3)(x + 3)$

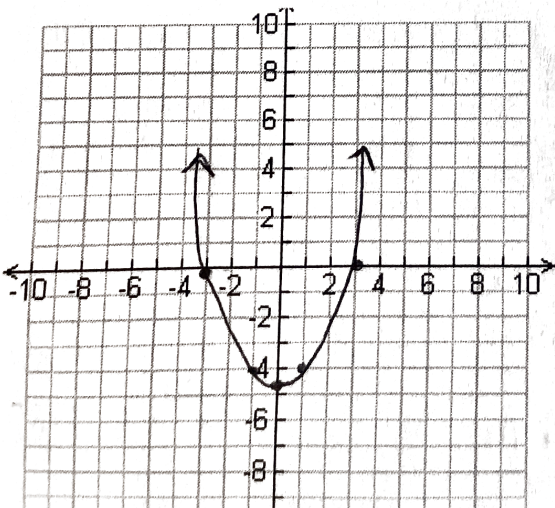
x-intercepts: $(3, 0)$ $(-3, 0)$

Axis of Symmetry is $x = 0$

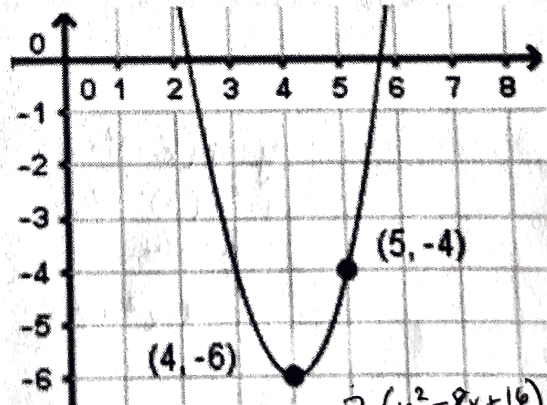
Vertex: $(0, -4.5)$

y-intercept: $(0, -4.5)$

Extra point: $(1, -4)$



4) Write each equation



$2(x^2 - 8x + 16) - 6$
 $2x^2 - 16x + 32 - 6$

Standard Form: $y = 2x^2 - 16x + 26$

Vertex Form: $y = 2(x - 4)^2 - 6$

Intercept Form: _____