

1. What is the domain and range of the function? Interval notation
2. What is the value of  $f(3)$ ?
3. What is the value of  $x$  when  $f(x) = 0$ ?
4. What is the maximum?



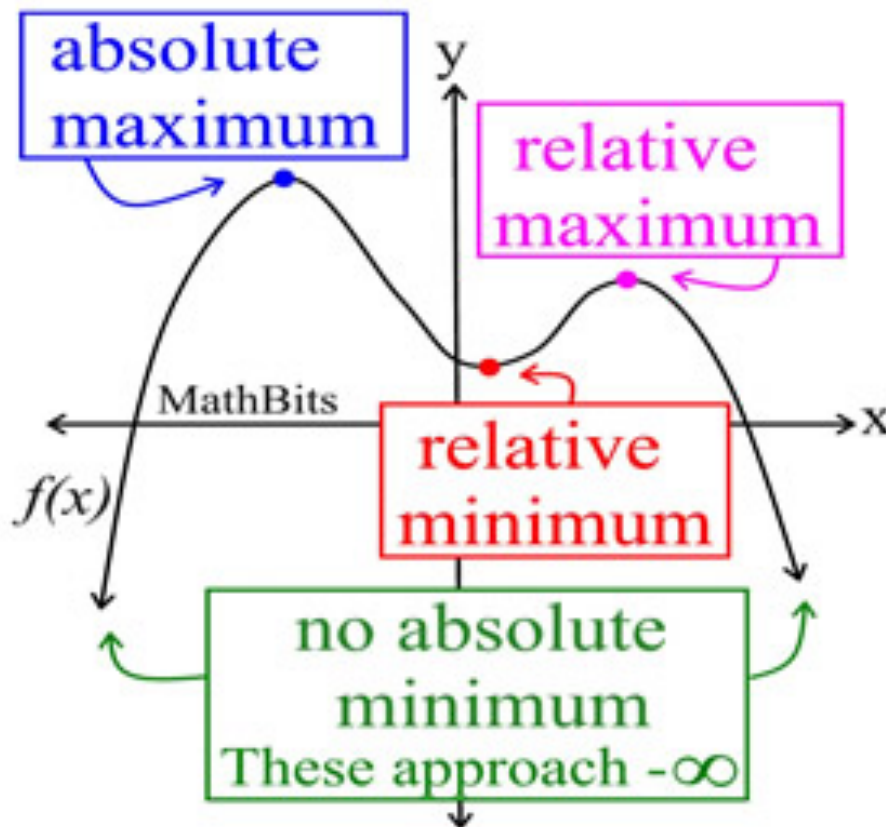
**Check Homework**

# Features We Have Discussed

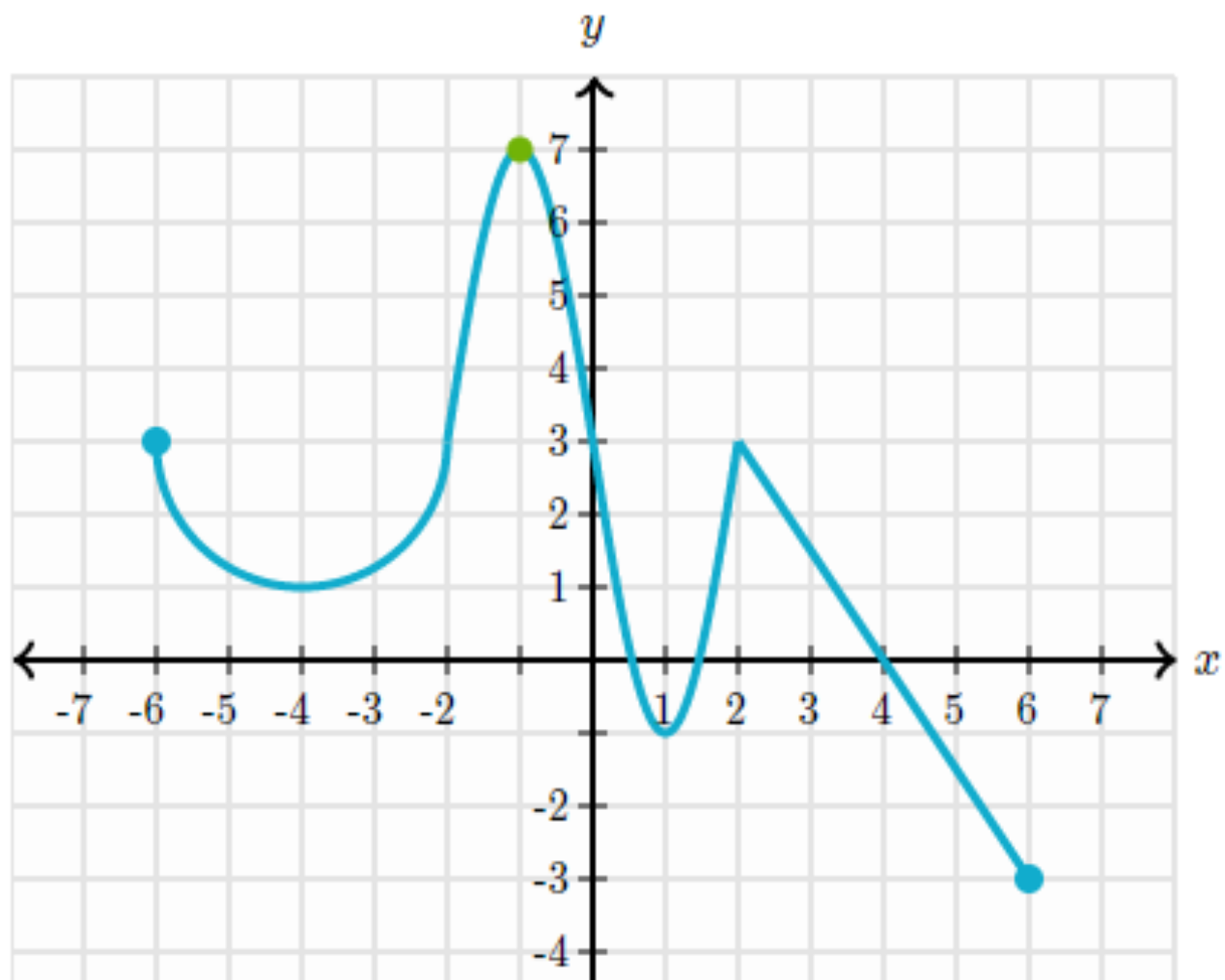
- Domain and Range
  - End Behavior
    - Increasing
    - Decreasing
  - X-Intercept
  - Y-Intercept
  - **Maximum**
  - **Minimum**
- **Average Rate of Change**

# Maximum and Minimums

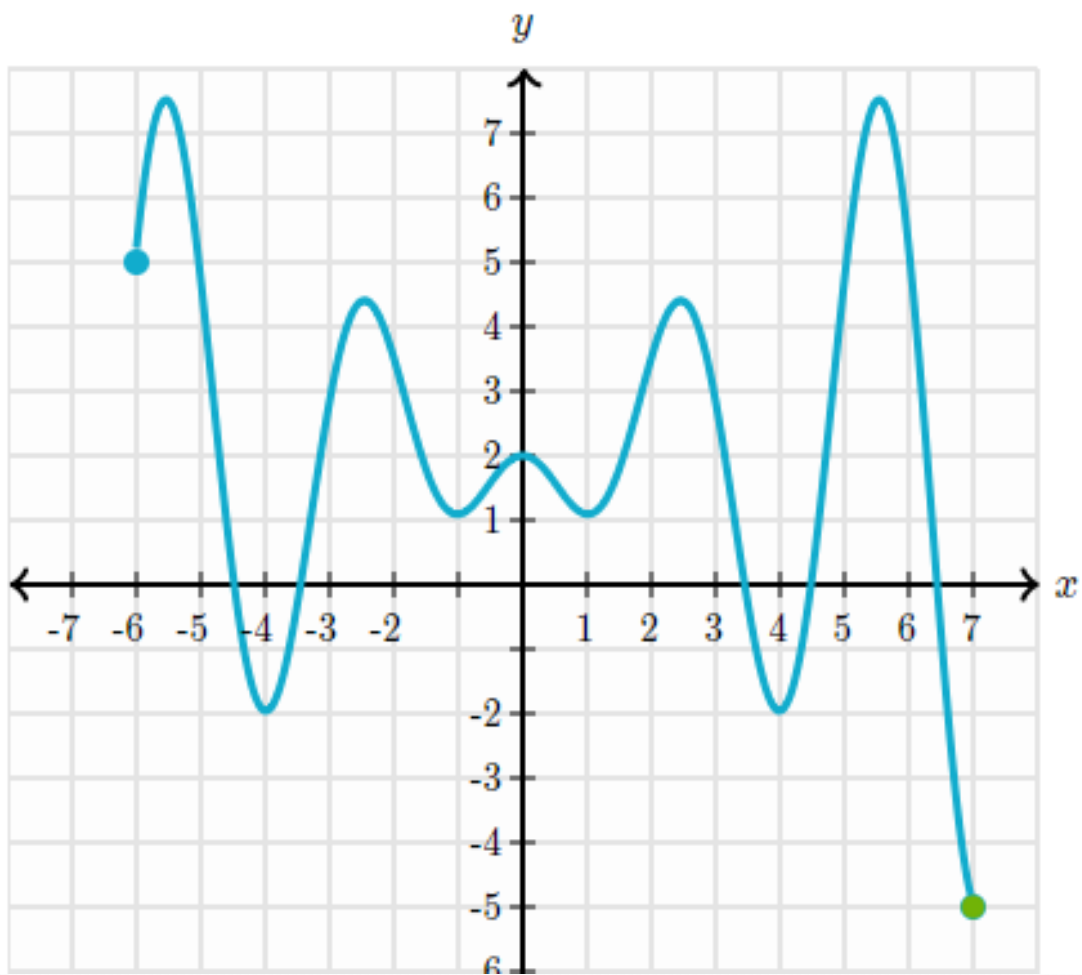
<https://www.khanacademy.org/math/algebra/algebra-functions/maximum-and-minimum-points/e/recognize-maxima-and-minima>



Mark the *absolute maximum* point of the graph.



Mark the *absolute minimum* point of the graph.



# Average Rate of Change

- <https://www.youtube.com/watch?v=lQRiw264bnI>

# Rate of Change

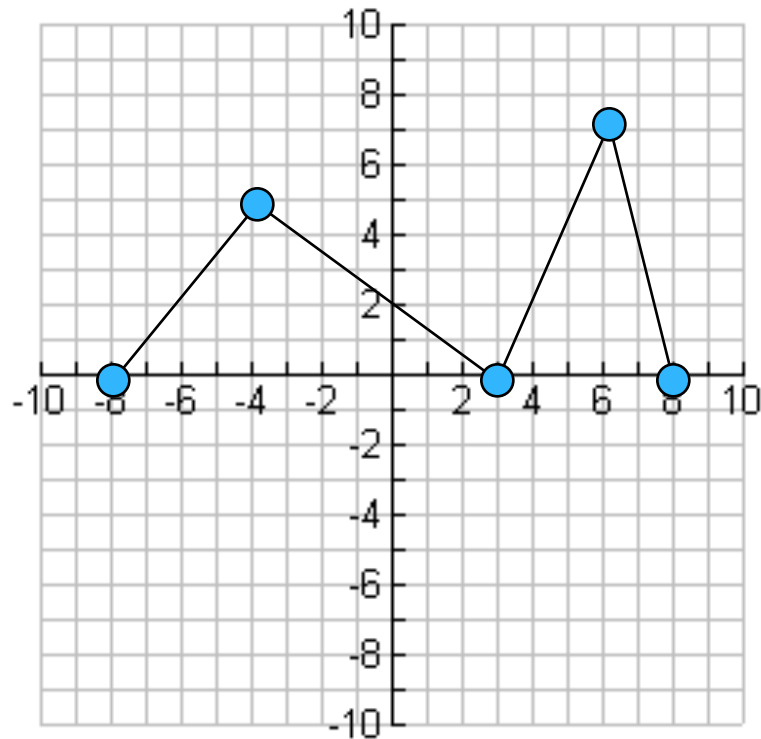
- ▶ The **rate of change** is the ratio of the change of one quantity to a change in another quantity.
- ▶ Example:
  - The table shows the amount of water evaporating from a swimming pool on a hot day. Find the rate of change in gallons with respect to time.

Time (hours)	2	6	12
Gallons evaporated	4.5	13.5	27



# Rate of Change

- Where is the greatest rate of change on the graph? What is the value?



# What kind of function do you find slope for?

- We only find slope for linear functions
- The slope of a line does not change no matter where you find it on the line.
- This is called constant rate of change

What do we do for other types of functions?

- Find the **average rate of change** in a specific interval. (It will change for each different interval!)

# Average Rate of Change

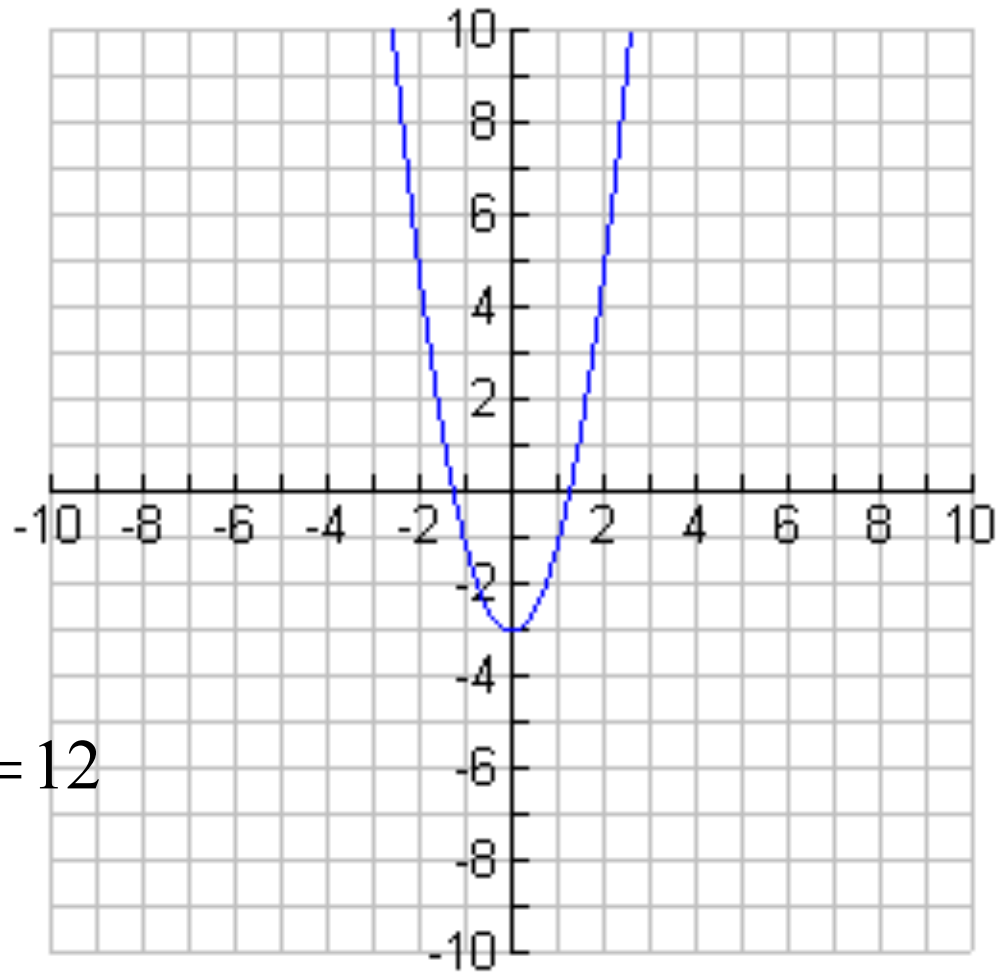
- The **average rate of change** between any two points  $(x_1, f(x_1))$  and  $(x_2, f(x_2))$  is the change of  $y$  over the change in  $x$  at the two endpoints of the interval.

$$m = \frac{y_2 - y_1}{x_2 - x_1} \quad \text{becomes} \quad \frac{f(x_2) - f(x_1)}{x_2 - x_1}$$

# Example 1

- Find the average rate of change of  $f(x) = 2x^2 - 3$  from  $x = 2$  to  $x = 4$ .

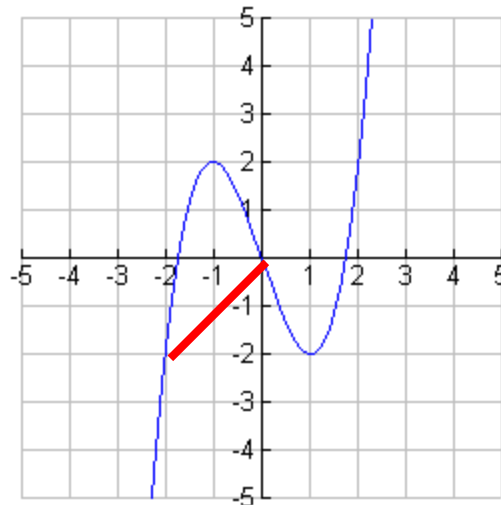
$$\begin{aligned}\frac{f(x_2) - f(x_1)}{x_2 - x_1} &= \frac{f(4) - f(2)}{4 - 2} \\ &= \frac{29 - 5}{4 - 2} = \frac{24}{2} = 12\end{aligned}$$



# Example 2

- Find the average rate of change of  $f(x) = x^3 - 3x$  from  $x = -2$  to  $x = 0$ .

$$\frac{f(x_2) - f(x_1)}{x_2 - x_1} = \frac{f(0) - f(-2)}{0 - (-2)} = \frac{0 - (-2)}{2} = \frac{2}{2} = 1$$





# Worksheet



# Homework

- Worksheet