

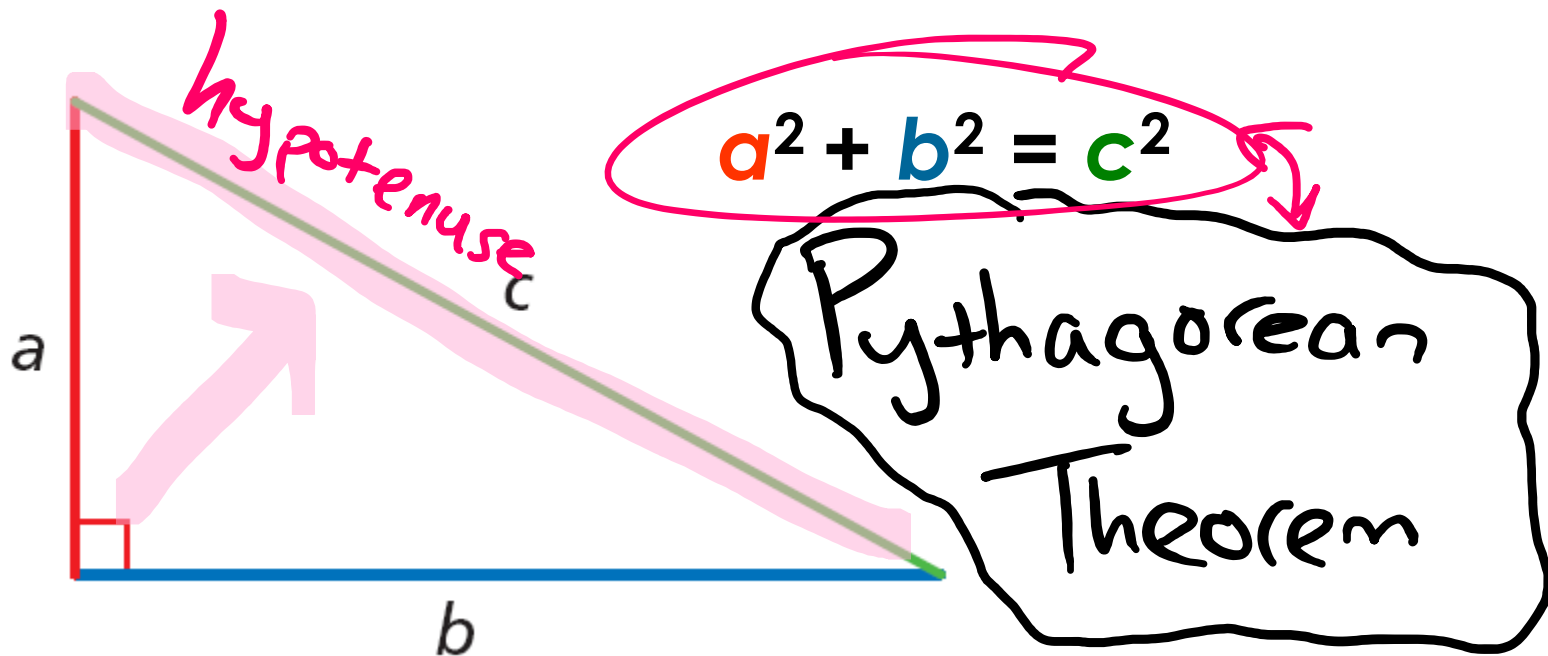
**Need a Calculator and Homework Out**

# Check Homework

Objective:

# Right Triangles and Pythagorean Multiples

In a right triangle, the sum of the squares of the lengths of the legs equals the square of the length of the hypotenuse.



# A Brief History

- The Pythagorean theorem takes its name from the ancient Greek mathematician **Pythagoras** (569 B.C.?-500 B.C.?), who was perhaps the first to offer a proof of the theorem. But people had noticed the special relationship between the sides of a right triangle long before Pythagoras.
- Although Pythagoras is credited with the famous theorem, it is likely that the **Babylonians** knew the result for certain specific triangles at least **a millennium earlier** than Pythagoras. It is not known how the Greeks originally demonstrated the proof of the Pythagorean Theorem. If the methods of Book II of Euclid's **Elements** were used, it is likely that it was a dissection type of proof similar to the following:

A proof of the Pythagorean Theorem using Similarity...

$$f^2 = de$$

$$b^2 = c \cdot e$$

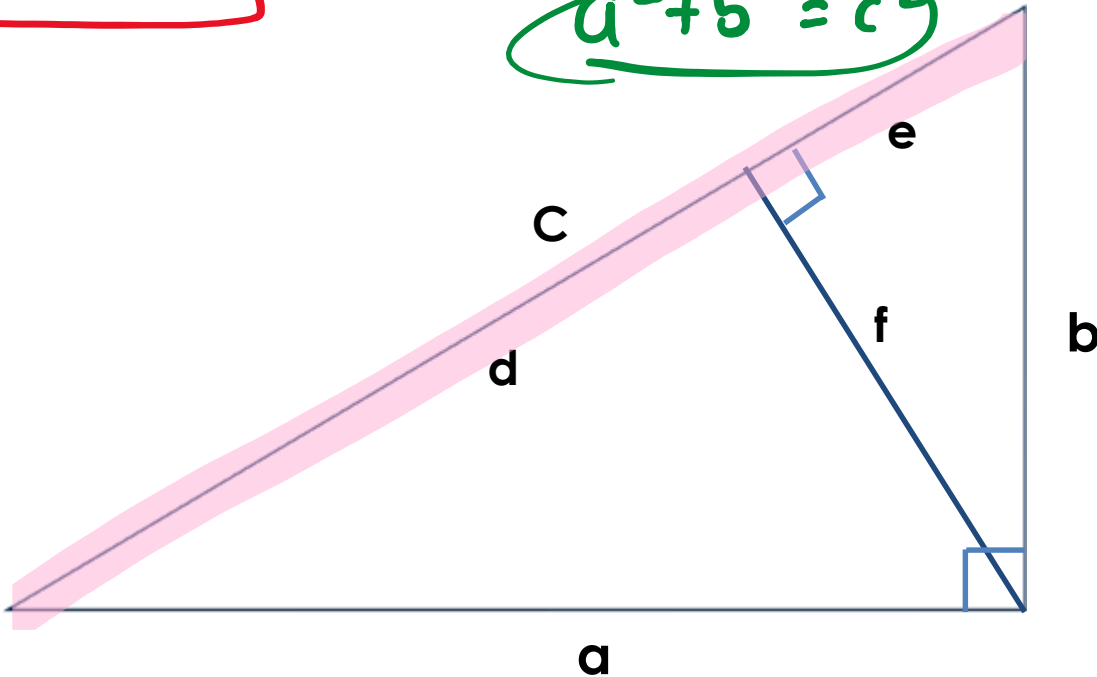
$$a^2 = d \cdot c$$

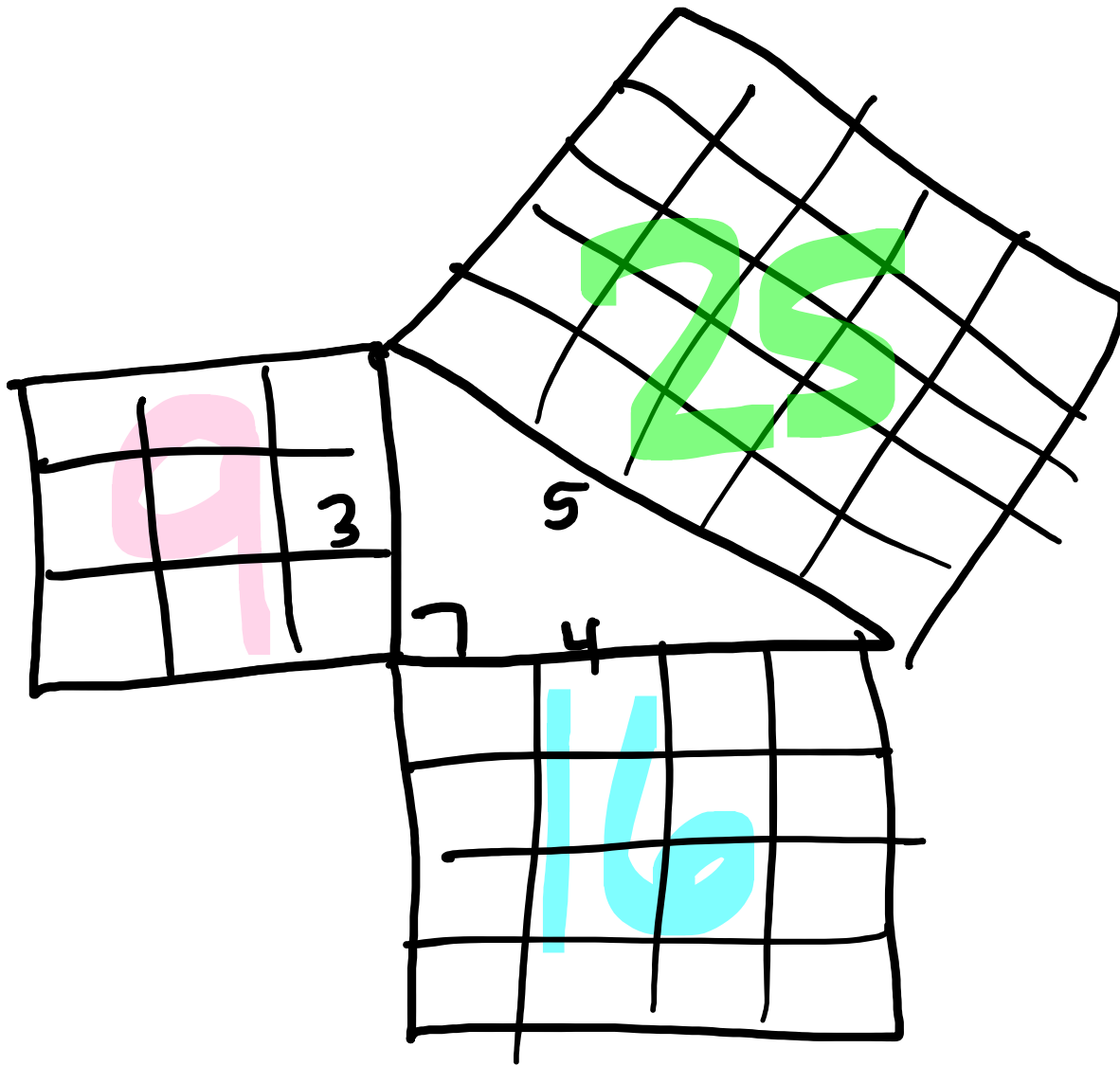
$$a^2 + b^2 = ce + dc$$

$$a^2 + b^2 = c(e + d)$$

$$a^2 + b^2 = c \cdot c$$

$$a^2 + b^2 = c^2$$





There are *MANY* other proofs of  
the Pythagorean Theorem

<https://www.youtube.com/watch?v=CAkMUdeB06o&spfreload=10>



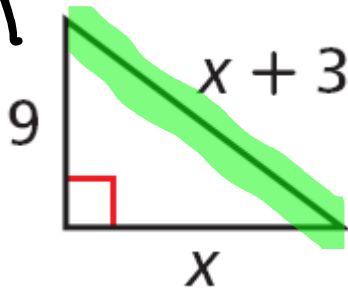
$$81 + \cancel{x^2} = \cancel{x^2} + 6x + 9$$

$$81 = 6x + 9$$

$$72 = 6x$$

$$\boxed{12 = x}$$

1. Find the value of  $x$ .



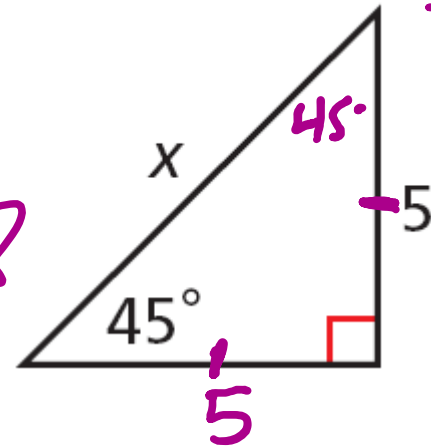
2.

$$5^2 + 5^2 = x^2$$

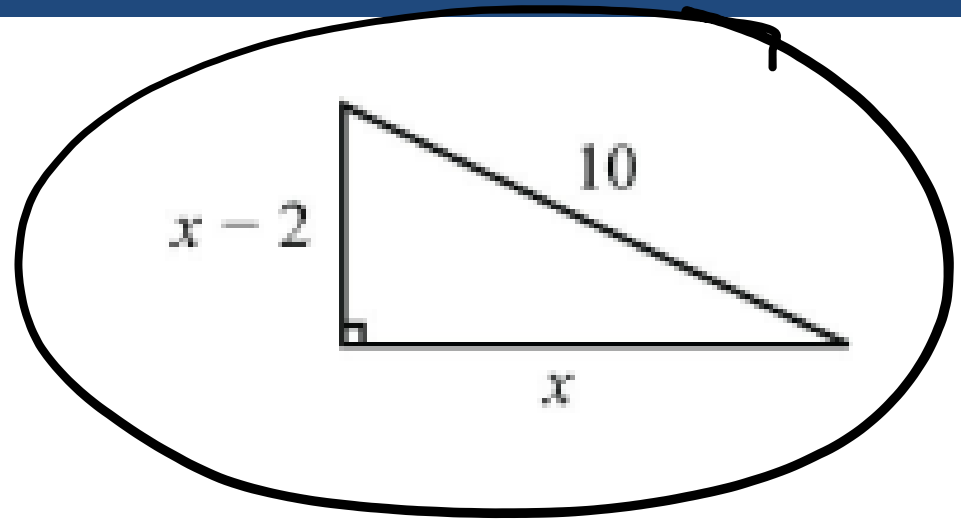
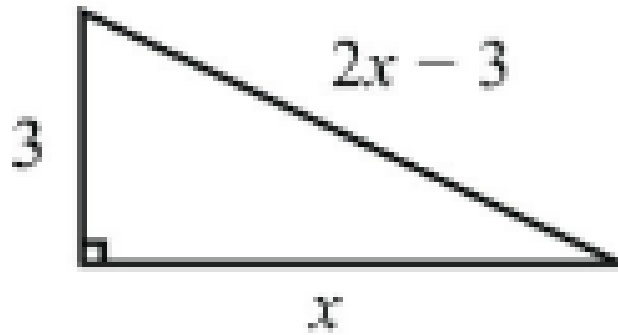
$$50 = x^2$$

$$\sqrt{50} = x$$

$$\boxed{5\sqrt{2} = x}$$



3. An entertainment center is 52 in. wide and 40 in. high. Will a TV with a 60 in. diagonal fit in it? Explain.



Find the value of  $x$  for each.



3 whole #s that satisfy the Pythagorean Theorem

A set of three nonzero whole numbers  $a$ ,  $b$ , and  $c$  such that  $a^2 + b^2 = c^2$  is called a Pythagorean triple.

### Common Pythagorean Triples

3, 4, 5

5, 12, 13

8, 15, 17

7, 24, 25

I expect you to know these four!

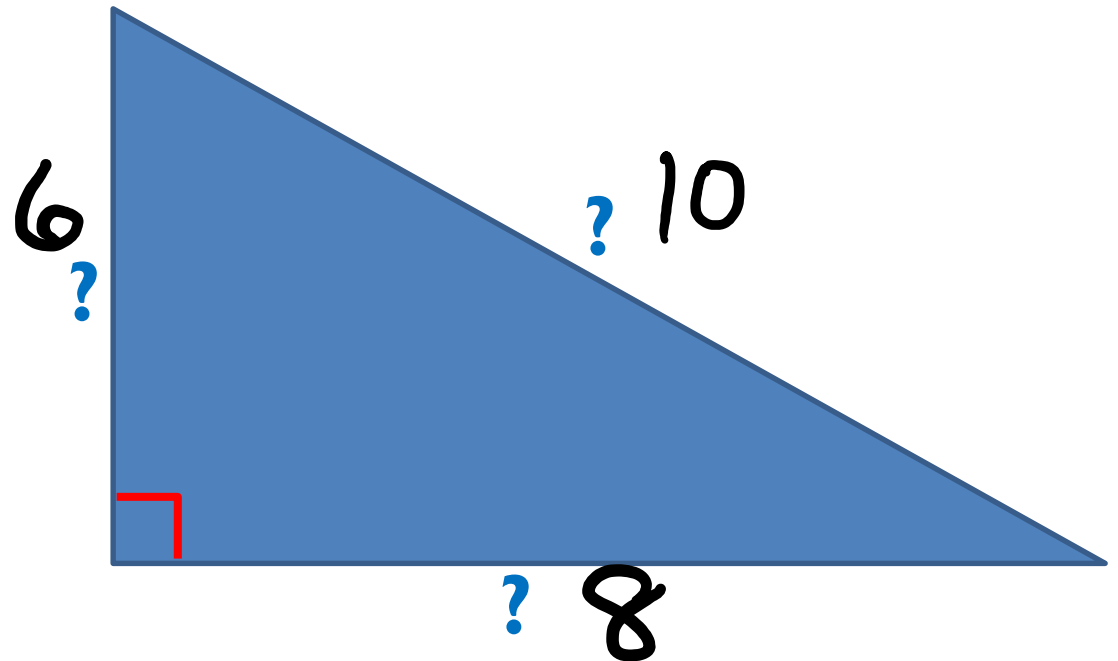
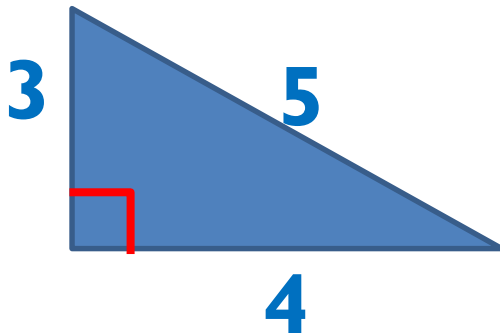
→  $3^2 + 4^2 = 5^2$

$5^2 + 12^2 = 13^2$

# If 3, 4, 5 works...

- Could you tell me the lengths of the sides of a triangle that would be similar to this triangle?

Pythagorean Multiples



# Common Pythagorean Triples

▣ 3, 4, 5

▣ 5, 12, 13

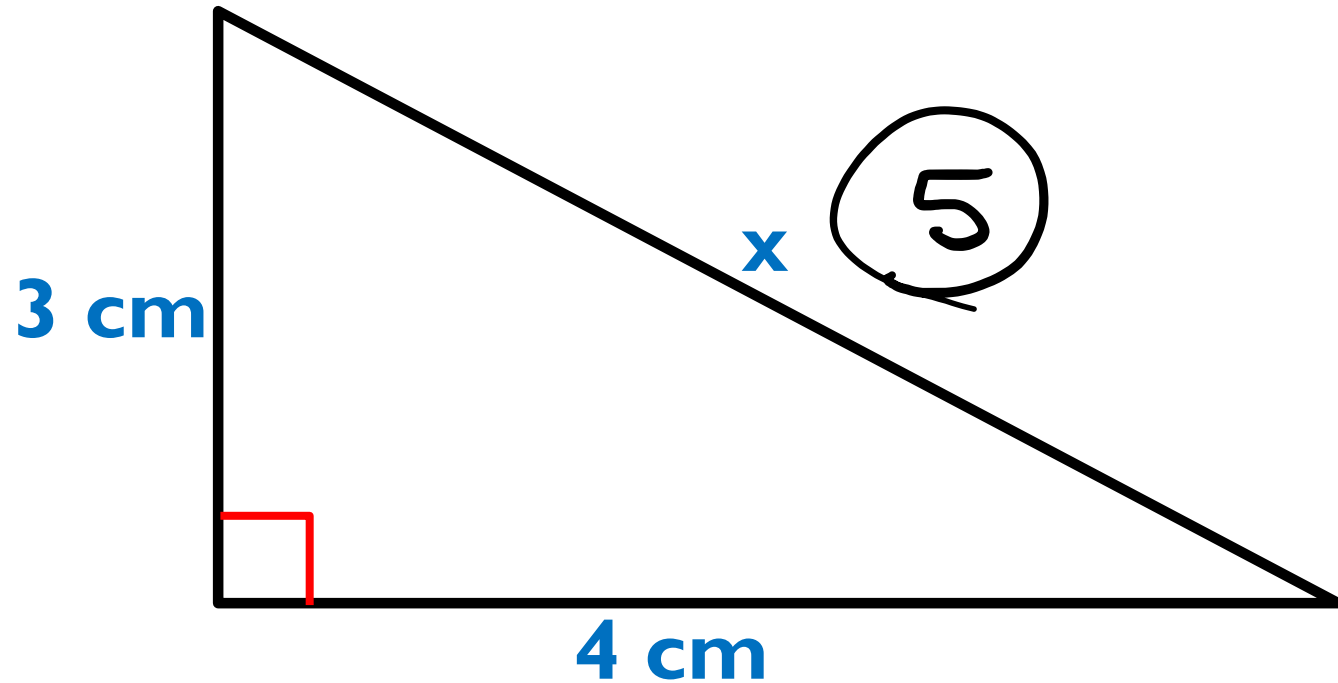
▣ 8, 15, 17

▣ 7, 24, 25

▣ + any multiple of these!

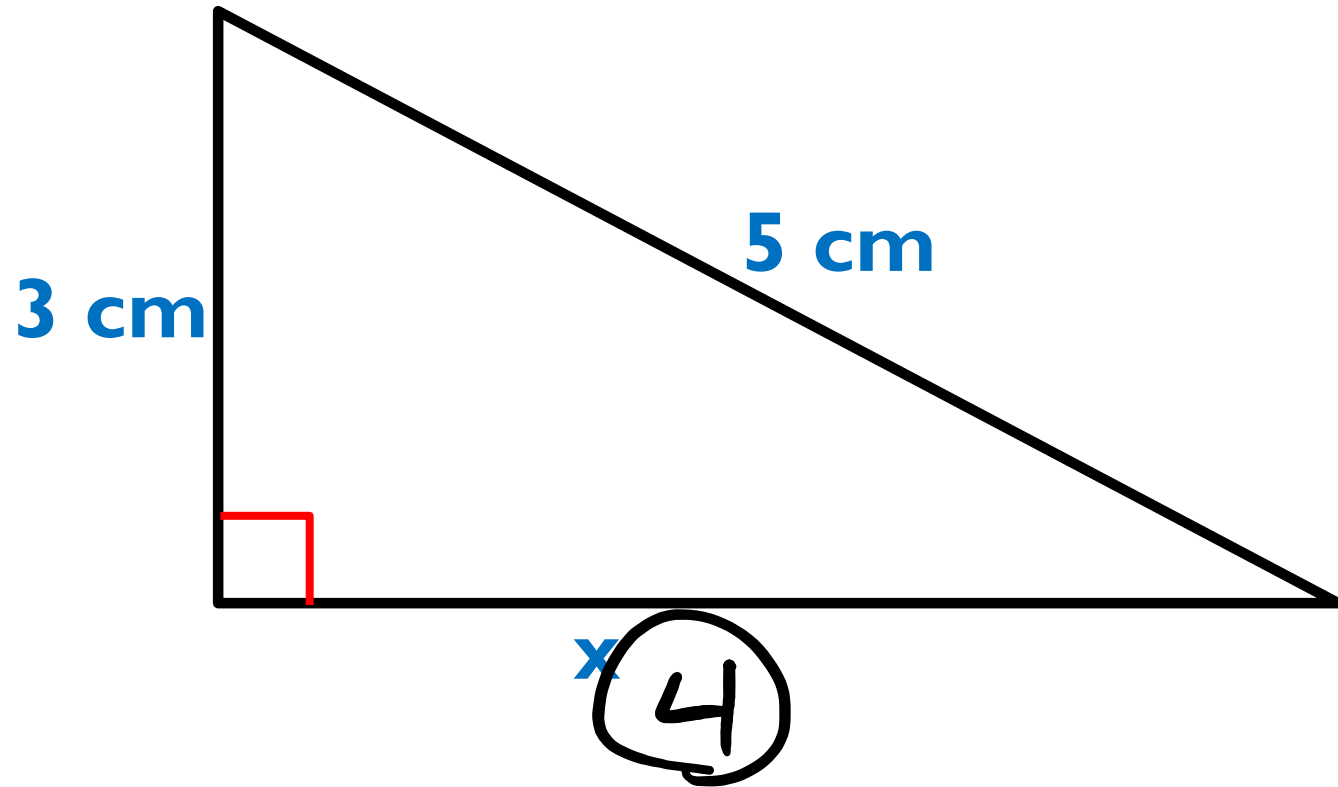
- 3, 4, 5  $\xrightarrow{\text{x2}}$  6, 8, 10
- 3, 4, 5  $\xrightarrow{\text{x3}}$  9, 12, 15
- 3, 4, 5  $\xrightarrow{\text{x6}}$  18, 24, 30
- 3, 4, 5  $\xrightarrow{\text{x100}}$  300, 400, 500

Find the length of the side!

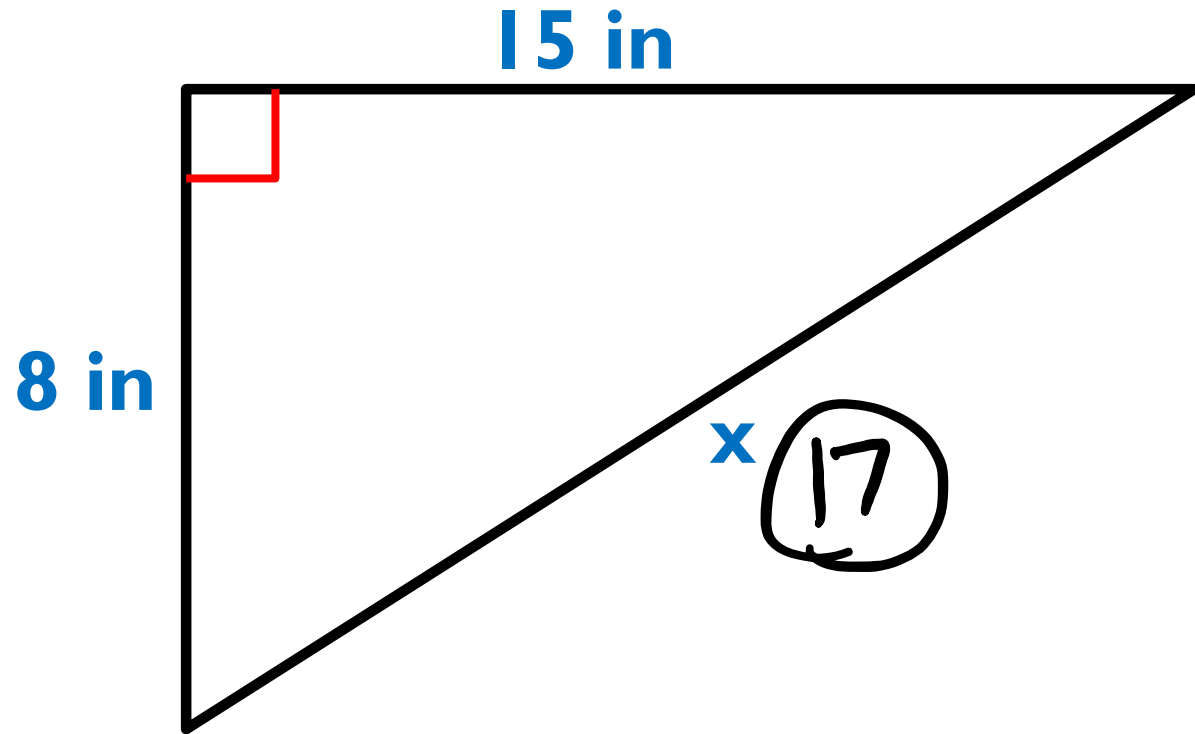




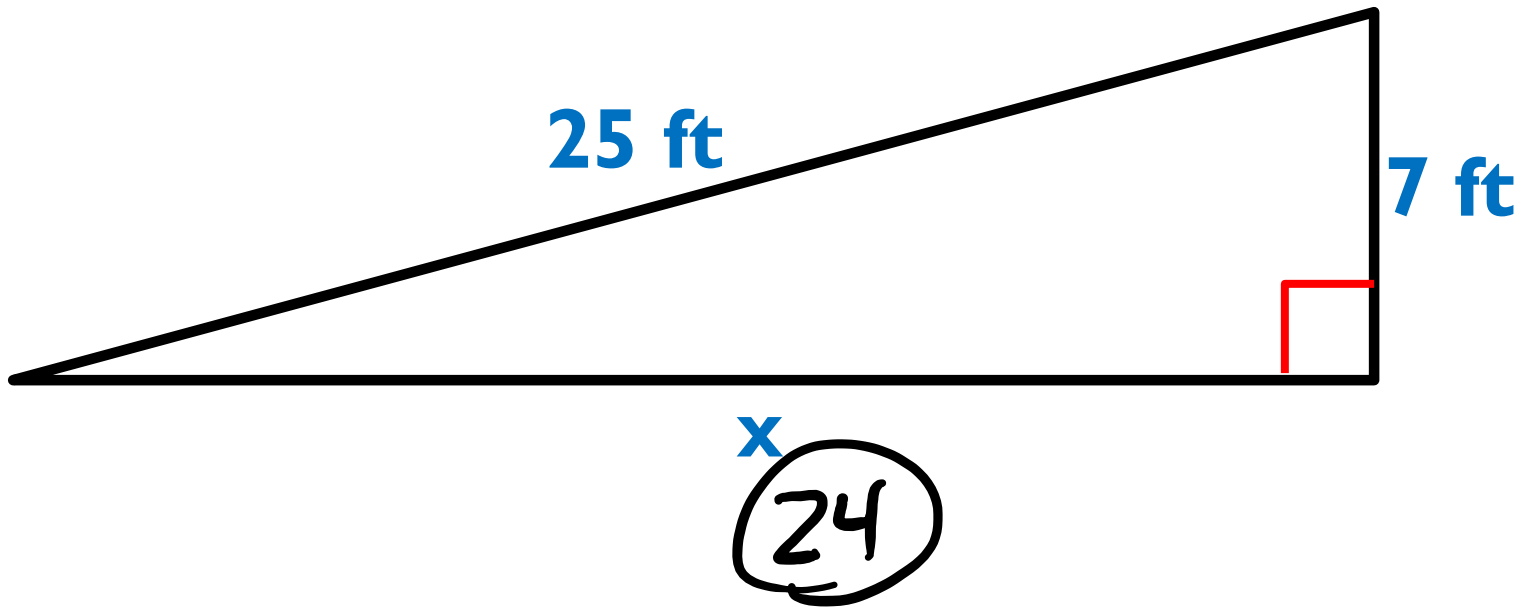
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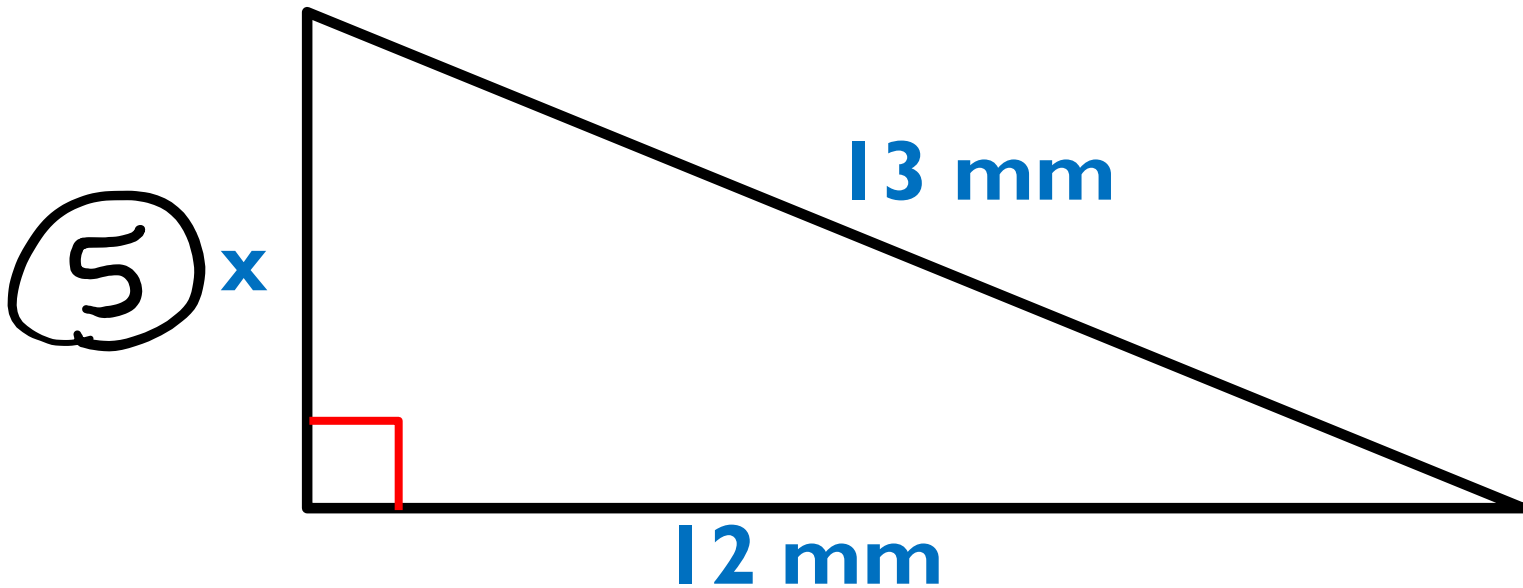
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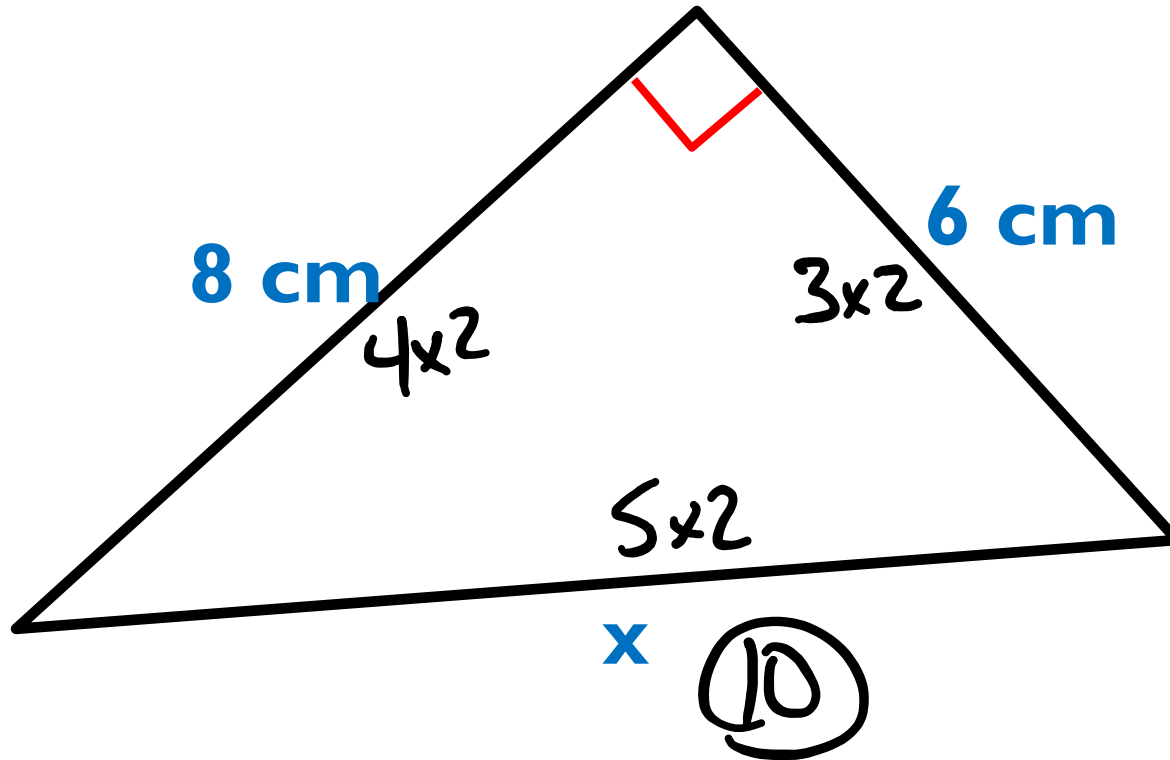
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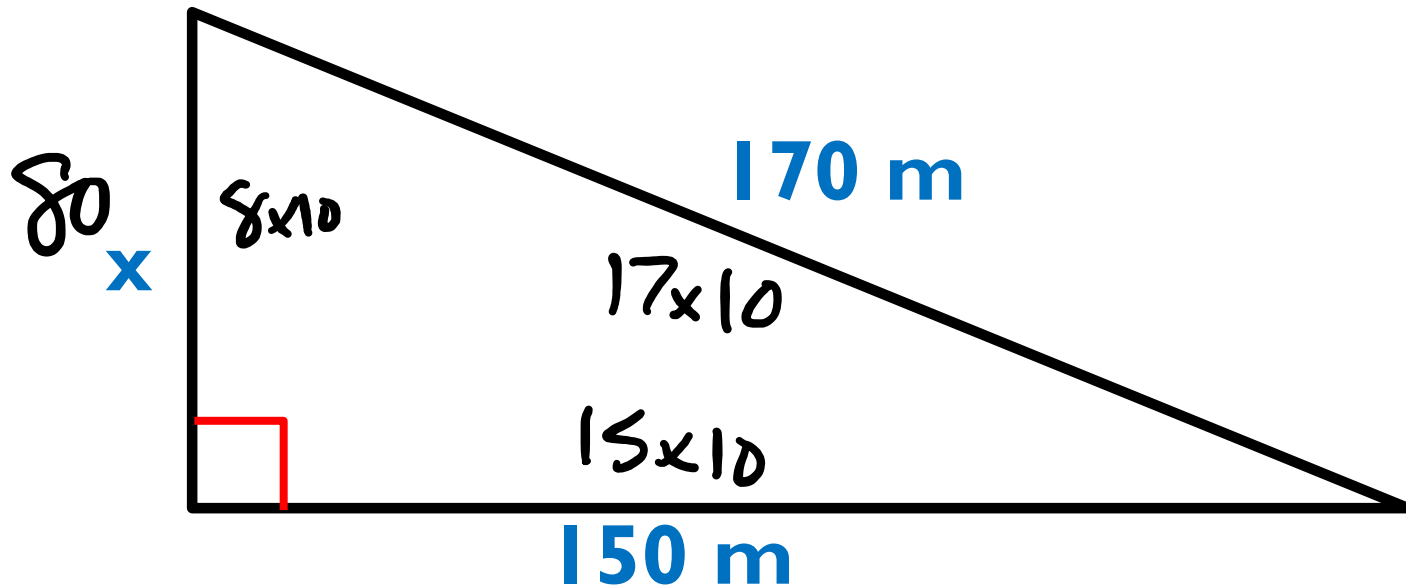
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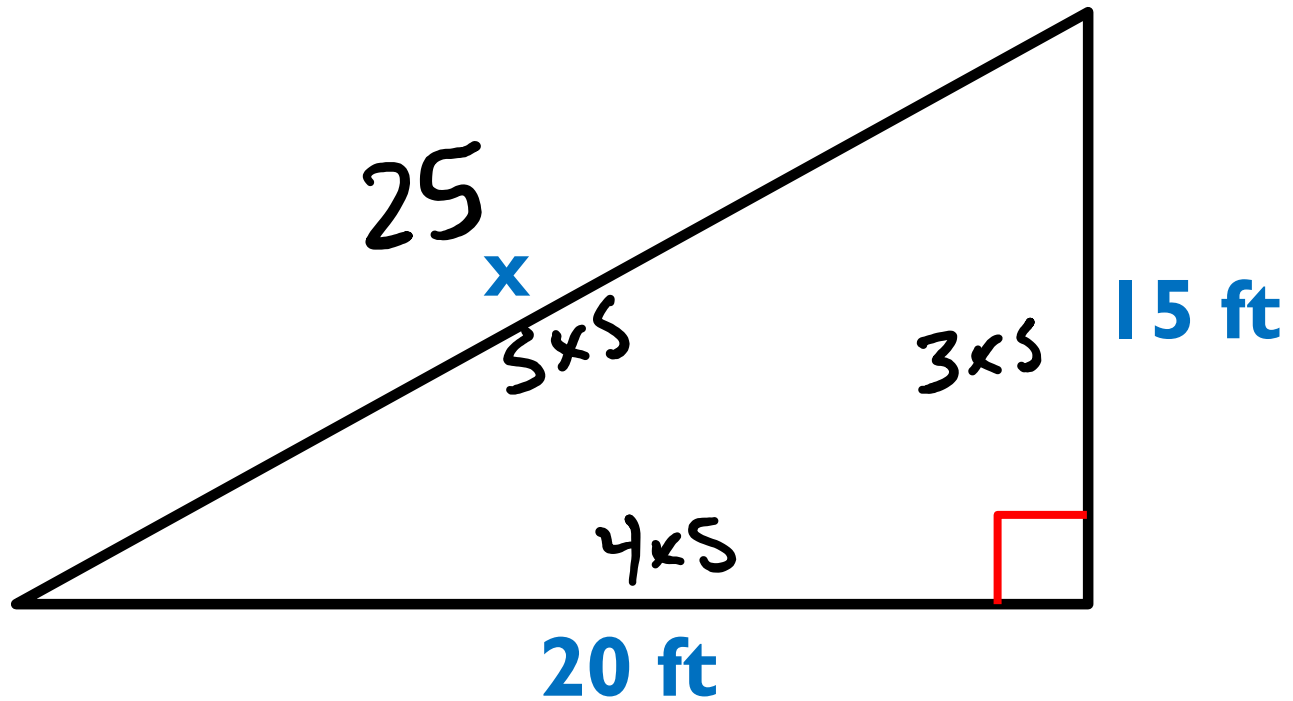
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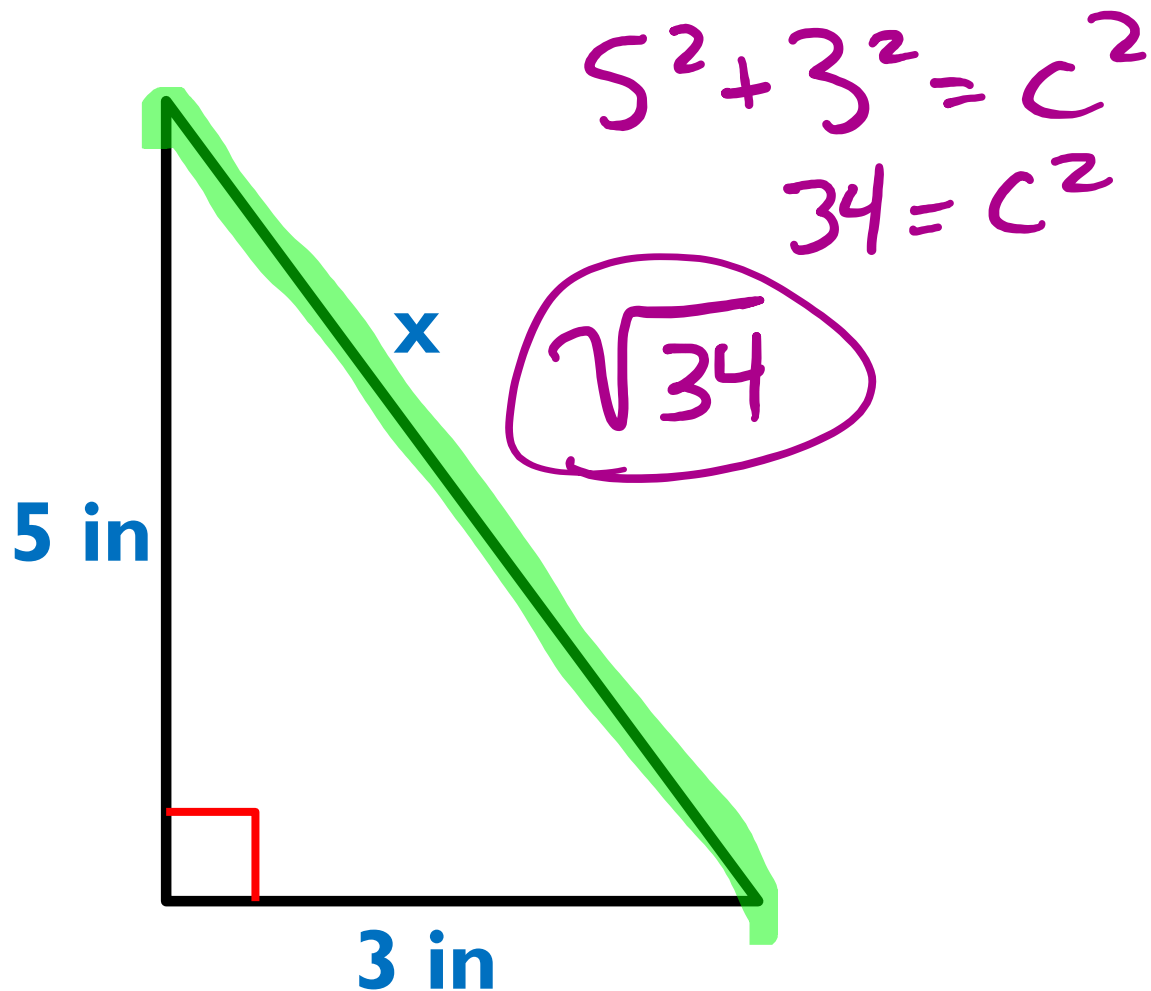
Find the length of the side!



Find the length of the side!

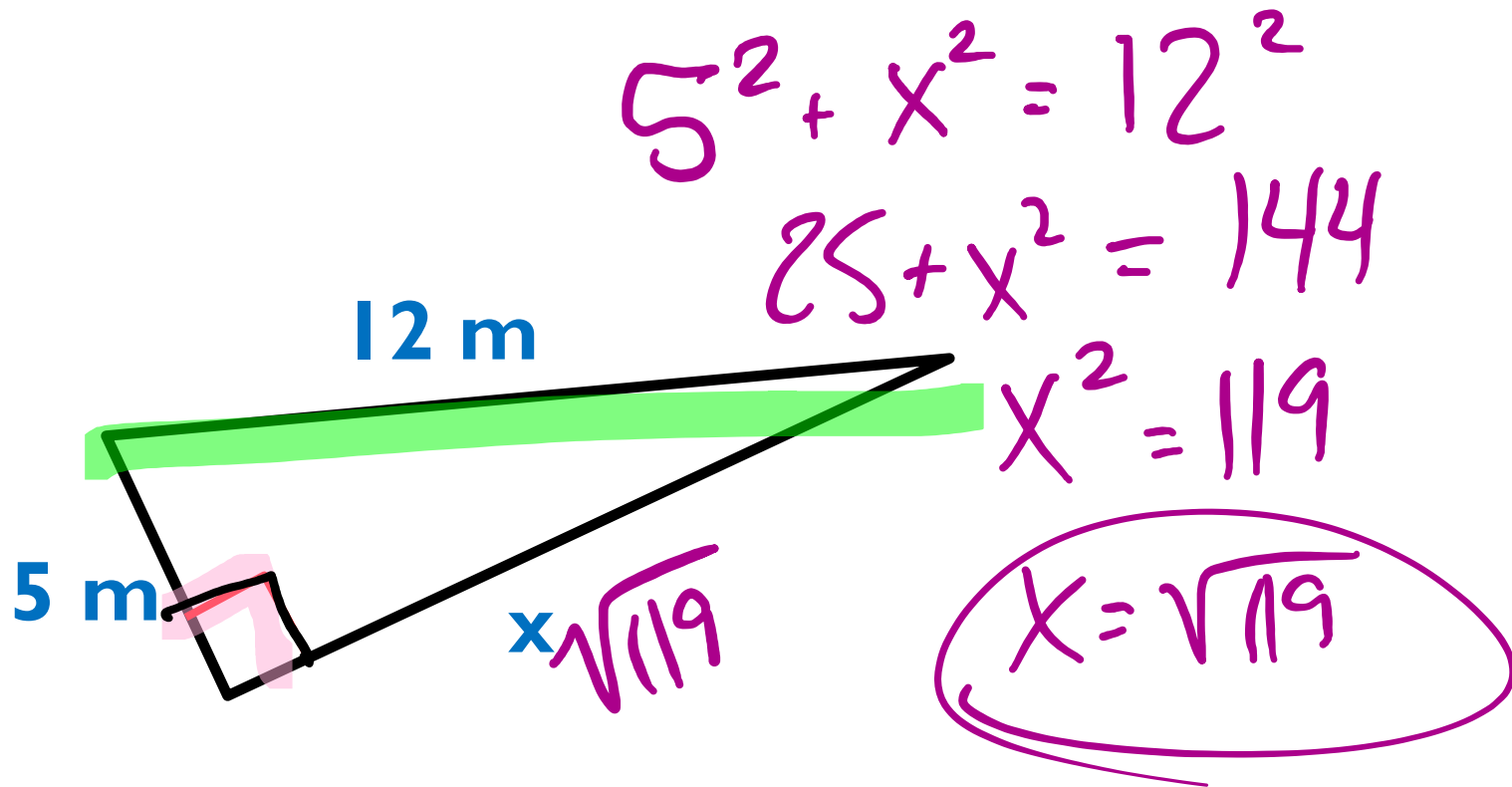


Find the length of the side!





Find the length of the side!



# Homework: Worksheet